



The Loop equations were

$$\begin{aligned}
 -I_1 R_1 - I_1 R_2 - I_3 R_4 + \varepsilon_1 - \varepsilon_3 &= 0 \\
 -I_1(R_1 + R_2) - I_3 R_4 + \varepsilon_1 - \varepsilon_3 &= 0 && \text{(Loop I)} \\
 -I_2 R_3 + I_3 R_4 - \varepsilon_2 + \varepsilon_3 &= 0 && \text{(Loop II)}
 \end{aligned}$$

The nodal equation is

$$I_1 - I_2 - I_3 = 0 \quad \text{(Nodal Eqn.)}$$

Using the values $\varepsilon_1 = 19V$; $\varepsilon_2 = 6V$; $\varepsilon_3 = 2V$ and $R_1 = 6\Omega$; $R_2 = 4\Omega$; $R_3 = 4\Omega$; $R_4 = 1\Omega$ we get the following equations:

$$-10 I_1 - I_3 = -17 \quad (1)$$

$$-4 I_2 + I_3 = 4 \quad (2)$$

$$I_1 - I_2 - I_3 = 0 \quad (3)$$

Solving Equation 1 for I_1 , we get

$$I_1 = \frac{-17 + I_3}{-10} \quad (4)$$

Solving equation 2 for I_2 , we get

$$I_2 = \frac{4 - I_3}{-4} \quad (5)$$

Now substitute Equations 4 and 5 into Equation 3 to get

$$\frac{17 - I_3}{10} + \frac{4 - I_3}{4} - I_3 = 0 \quad (6)$$

Now multiply Equation 6 by 40 to get

$$\begin{aligned}
 68 - 4 I_3 + 40 - 10 I_3 - 40 I_3 &= 0 \\
 54 I_3 &= 108 \\
 I_3 &= 2 \text{ Amps}
 \end{aligned} \quad (7)$$

Now substitute this into Equations 4 and 5 to get

$$I_1 = \frac{-17 + 2}{-10} = 1.5 \text{ Amps} \quad (8)$$

$$I_2 = \frac{4 - 2}{-4} = -0.5 \text{ Amps in the direction opposite to that indicated} \quad (9)$$